College Mathematics
numerical comparisons
LAND AREA POPULATION
(in square miles)

| Australia | $2,900,000$ | $22,600,000$ |
| :--- | ---: | ---: |
| Bangladesh | 57,000 | $160,000,000$ |
| Brazil | $3,300,000$ | $190,000,000$ |
| Canada | $3,600,000$ | $34,400,000$ |
| China | $3,500,000$ | $1,300,000,000$ |
|  |  |  |
| France | 247,000 | $65,000,000$ |
| Japan | 146,000 | $130,000,000$ |
| Germany | 138,000 | $80,000,000$ |
| India | $1,150,000$ | $1,200,000,000$ |
| Indonesia | 705,000 | $230,000,000$ |
|  |  |  |
| Mexico | 742,000 | $110,000,000$ |
| Pakistan | 307,000 | $170,000,000$ |
| Russia | $6,300,000$ | $140,000,000$ |
| United Kingdom | 95,000 | $60,000,000$ |
| United States | $3,500,000$ | $310,000,000$ |

Answer each of the following questions three different ways:
(a) using a multiplier [Germany is 0.559 times as big as France.]
(b) as a percent of the reference [Germany's land area is $55.9 \%$ of France's.]
(c) using a percent difference
[Germany's land area is $44.1 \%$ less than France's.]
Round multipliers to the nearest thousandth and percentages to the nearest tenth of a percent.

1. How big is Canada, compared to the United States?
2. How big is India, compared to the United States?
3. How big is Mexico, compared to the United States?
4. How big is Russia, compared to the United States?
5. How big is the United Kingdom, compared to the United States?
6. How big is Bangladesh, compared to India?
7. How big is India, compared to Pakistan?
8. How big is Pakistan, compared to Bangladesh?
9. How populous is Canada, compared to the United States?
10. How populous is China, compared to the United States?
11. How populous is Indonesia, compared to the United States?
12. How populous is Mexico, compared to the United States?
13. How populous is Russia, compared to the United States?
14. How populous is Bangladesh, compared to India?
15. How populous is India, compared to Pakistan?
16. How populous is Pakistan, compared to Bangladesh?

QUESTIONS TO ASK:
What is the main thing discussed? (subject)
To what is it being compared?
What is the change?
(reference)
(difference)
How big is the reference?
How big is the change?
How big is the subject?
How big is the reference?
How big is the change?
How big is the subject?
reference $/$ reference $=1$
difference / reference
subject / reference
$100 \%$ of the reference
$\mathrm{P} \%$ of the reference
$(100+P) \%$ of the reference, if the change is a decrease
$(100-\mathrm{P}) \%$ of the reference, if the change is an increase
EXAMPLE 1:
The price of Photon Industries stock went from \$50 to \$157.
Compare the final price to the original price.

What is the main thing discussed?
To what is it being compared?
What is the change?
How big is the original price?
How big is the price increase?
How big is the final price?
How big is the original price?
How big is the price increase?
How big is the final price?
final price (\$157)
original price (\$50)
price increase (\$107)
1 of the original price
2.14 of the original price
3.14 of the original price
$100 \%$ of the original price
$214 \%$ of the original price
$314 \%$ of the original price

## EXAMPLE 2:

The price of Quantum Computers stock went from $\$ 400$ to $\$ 3$. Compare the final price to the original price.

What is the main thing discussed?
To what is it being compared?
What is the change?
How big is the original price?
How big is the price decrease?
How big is the final price?
How big is the original price?
How big is the price decrease?
How big is the final price?
final price (\$3)
original price (\$400)
price decrease (\$397)
1 of the original price
0.9925 of the original price
0.0075 of the original price

100\% of the original price
$99.25 \%$ of the original price
$0.75 \%$ of the original price

