Test 3 may include review problems from earlier sections so restudy the test 1 and test 2 reviews also (especially solving systems of equations and the equations for lines).

NOTE: In addition to the problems below, please study the handout for Exercise Set 5.2 and review earlier sections.

1. Solve the system of equations by graphing. If there is no solution or more than one solution, state this.

$$
\begin{aligned}
& 6 x-3 y=12 \\
& y=2 x-4
\end{aligned}
$$

2. Solve the system of equations by graphing. If there is no solution or more than one solution, state this. (A brief note: Any time I ask you to solve a system of equations, if there is no solution or more than one solution, you must tell me this, even if I don't specifically ask about it.)

$$
\begin{aligned}
& x-y=6 \\
& 2 x-2 y=-6
\end{aligned}
$$

3. Solve the system of equations by graphing.

$$
\begin{aligned}
& 2 x+y=10 \\
& 3 x+2 y=18
\end{aligned}
$$

4. Solve the system of equations by using the substitution method.

$$
\begin{aligned}
& x=3 y+5 \\
& 4 x-12 y=20
\end{aligned}
$$

5. Solve the system of equations by using the elimination method.

$$
\begin{aligned}
& 2 x-10 y=1 \\
& 3 x-15 y=4
\end{aligned}
$$

6. Solve the system of equations. (You may use whichever method you like if I don't tell you one to use. Hint: The graphing method is usually not a good choice unless I specifically ask you for it.)

$$
\begin{aligned}
& 4 y-x=27 \\
& 2 x+7 y=21
\end{aligned}
$$

7. Solve the system of equations.

$$
\begin{aligned}
& 4 x+y=-2 \\
& 3 y-2 x=-13
\end{aligned}
$$

8. Solve the system of equations.

$$
\begin{aligned}
& 4 x+5 y=3 \\
& 6 x-3 y=15
\end{aligned}
$$

9. Solve the system of equations.
$5 x-4 y=2$
$11 x+2 y=8$
10. Simplify: $57 \cdot 5^{2}$
11. Simplify: $\left(-6 a b^{5} C^{3}\right)\left(-3 a^{2} c^{5}\right)$
12. Simplify: $-4 x^{2} y z^{3} \cdot 7 w x y z^{2}$
13. Simplify: $y^{16} \div y^{9}$
14. Simplify: $\frac{3^{10}}{3^{6}}$
15. Simplify: $\frac{14 w^{2} x^{4} y^{6} z^{0}}{21 w^{8} x^{4} y^{3} z^{5}}$
16. Simplify: $\left(11^{4}\right)^{6}$
17. Simplify: $\left(-4 x y^{4}\right)^{3}$
18. Simplify: $\left(-2 a^{2} b^{5}\right)^{4}$
19. Simplify: $\left(5 v^{5} w^{3}\right)\left(-2 v^{2} w^{5}\right)^{3}$
20. Simplify: $4^{0}$
21. Simplify: $5 x^{0}$
22. Simplify: $(5 x)^{0}$
23. Identify each polynomial below as a monomial, a binomial, or a trinomial and indicate its degree.
a. $\quad 10+3 z^{4}-9 z^{3}$
b. $\quad 19 m^{15}$
c. $x+2 x^{5}-4$
d. $\quad 100-5 y$
e. -8
24. Evaluate $2 u^{3} v-5 u v+3 u-v+10$ when $u=2$ and $v=-5$.
25. Simplify: $\left(11 x^{3}+4 x^{2}-5 y^{3}-3 y\right)+\left(2 x^{3}-4 x^{2}+y\right)$
26. Simplify: $\left(7 y^{2}-2 x+y\right)-\left(4 y^{2}-3 y+2 x\right)$
27. Simplify: $3 x y^{3}\left(5 x^{3}-7 x y^{2}+x y-2 y\right)$
28. Divide: $\frac{12 x y^{6}+24 x^{5} y^{9}}{4 x y^{3}}$
29. Divide: $\frac{20 r^{3} s^{2} t-4 r s^{2} t}{12 r^{2} s t^{3}}$
30. Divide: $\left(12 x^{2}-7 x-13\right) \div(3 x+2)$
31. Divide: $\left(x^{3}-11 x+6\right) \div(x-3)$
32. Divide: $\left(3 x^{3}+4 x^{2}+8\right) \div(x+2)$
33. Simplify: $(w-5)(w-7)$
34. Simplify: $(8 y+1)(2 y-7)$
35. Simplify: $(2 y+3)^{2}$
36. Simplify: $(w-4)^{2}$
37. Simplify: $(6 r-7 s)^{2}$
38. Simplify: $(3 x-4)(3 x+4)$
39. Simplify: $(w+6 v)(w-6 v)$
40. Simplify: $(5 x-3)(2 y+9)$
41. Simplify: $\left(4 a^{3}-3\right)\left(a^{3}-5 a+1\right)$
42. Evaluate: $x^{2}-y^{2}-z^{2}$ if $x=-5, y=6$, and $z=-4$
43. A car travels at a rate $94 \mathrm{~km} / \mathrm{h}$ slower than the rate of a train. In the same time that the car travels 329 km , the train travels 987 km . Find the speed of the car and the speed of the train.
44. The sum of two numbers is 21 . Half the larger number plus twice the smaller number is 12 . What are the numbers?
45. Ling had a total of $\$ 1482$ in her checking account and her savings account. Her savings account paid $4 \%$ in simple interest and her checking account paid $2.5 \%$ in simple interest. If she earned $\$ 51.42$ in interest for the year, how was her money
divided between the two accounts?
46. Ben has a total of 49 bills, consisting of $\$ 5$ bills and $\$ 10$ bills. If the total value of the bills is $\$ 350$, how many of each does he have?
47. Alan needs 250 ml of a solution that is $45 \%$ alcohol. If he has a solution that is $50 \%$ alcohol and purified water (which is $0 \%$ alcohol), how much of each should he mix together?
48. Jose wants 8 pounds of a dried fruit mixture that he can sell for $\$ 3.75$ per pound. If he has dried peaches that cost $\$ 4.50$ per pound and dried apples that cost $\$ 3.25$ per pound, how much of each should he use?
49. LaKeshia wants 400 ml of a solution that is $11 \% \mathrm{HCl}$. If she has only $8 \% \mathrm{HCl}$ and $16 \% \mathrm{HCl}$, how much of each should she mix together?
50. Darcy has 23 fewer quarters than dimes. Altogether the coins are worth $\$ 17.35$. How many of each does she have?
51. Two angles are complementary. One angle is $24^{\circ}$ less than twice the other. Find the angles. (Hint: complementary angles have a sum of $90^{\circ}$.)
52. A person's paycheck $P$ varies directly as the number of hours worked $H$. For 15 hr of work, the pay is $\$ 78.75$. Find the pay for 35 hr of work.
53. Simplify $6 y-4(y+3)+(y-4)$
54. Simplify $10 x y^{5}-\left(-7 x y^{5}\right)$

## ANSWERS:

1. Infinitely Many Solutions (Same Line - All points on the line are solutions.)

2. No Solution (Parallel Lines - They share no common points.)

3. $x=2$ and $y=6$, or $(2,6)$

4. Infinitely Many Solutions (Same Line - All points on the line are solutions.)
5. No Solution (Parallel Lines - They share no common points.)
6. $x=-7$ and $y=5$, or $(-7,5)$
7. $x=\frac{1}{2}$ and $y=-4$, or $\left(\frac{1}{2},-4\right)$
8. $x=2$ and $y=-1$, or $(2,-1)$
9. $x=\frac{2}{3}$ and $y=\frac{1}{3}$, or $\left(\frac{2}{3}, \frac{1}{3}\right)$
10. $5^{9}$
11. $18 a^{3} b^{5} c^{8}$
12. $-28 w x^{3} y^{2} z^{5}$
13. $y^{7}$
14. $3^{4}$
15. $\frac{2 y^{3}}{3 w^{6} z^{5}}$
16. $11^{24}$
17. $-64 x^{3} y^{12}$
18. $16 \mathrm{a}^{8} \mathrm{~b} 20$
19. $-40 v^{11} w^{18}$
20. 1
21. 5
22. 1
23. a. trinomial, 4
b. monomial, 15
C. trinomial, 5
d. binomial, 1
e. monomial, 0
24. -9
25. $13 x^{3}-5 y^{3}-2 y$
26. $3 y^{2}-4 x+4 y$
27. $15 x^{4} y^{3}-21 x^{2} y^{5}+3 x^{2} y^{4}-6 x y^{4}$
28. $3 y^{3}+6 x^{4} y^{6}$
29. $\frac{5 r s}{3 t^{2}}-\frac{\mathrm{s}}{3 r t^{2}}$
30. $4 \mathrm{x}-5+\frac{-3}{3 \mathrm{x}+2}$, or $4 \mathrm{x}-5-\frac{3}{3 \mathrm{x}+2}$
31. $x^{2}+3 x-2$
32. $3 x^{2}-2 x+4$
33. $w^{2}-12 w+35$
34. $16 y^{2}-54 y-7$
35. $4 y^{2}+12 y+9$
36. $w^{2}-8 w+16$
37. $36 r^{2}-84 r s+49 s^{2}$
38. $9 x^{2}-16$
39. $w^{2}-36 v^{2}$
40. $10 x y+45 x-6 y-27$
41. $4 a^{6}-20 a^{4}+a^{3}+15 a-3 f$
42. -27
43. The speed of the car is $47 \mathrm{~km} / \mathrm{h}$ and the speed of the train is $141 \mathrm{~km} / \mathrm{h}$.
44. The numbers are 1 and 20.
45. Ling began the year with $\$ 524$ in her checking account and $\$ 958$ in her savings account.
46. Ben has $28 \$ 5$ bills and $21 \$ 10$ bills.
47. Alan should mix 225 ml of the $50 \%$ alcohol and 25 ml of the purified water.
48. Jose should mix 3.2 pounds of dried peaches and 4.8 pounds of dried apples.
49. LaKeshia should mix 250 ml of $8 \% \mathrm{HCl}$ and 150 ml of $16 \% \mathrm{HCl}$.
50. Darcy has 43 quarters and 66 dimes.
51. The angles are $38^{\circ}$ and $52^{\circ}$.
52. The pay is $\$ 183.75$ for 35 hr of work.
53. $3 y-16$

MATD 0370 ELEMENTARY ALGEBRA REVIEW FOR TEST 3 (1.1-6.3)
54. $17 x y^{5}$

