

# SEQUENCES

<b><math>n^{\text{th}}</math> term of an arithmetic sequence</b>	In the arithmetic sequence with first term $a_1$ and common difference $d$ , the $n^{\text{th}}$ term, $a_n$ , is given by	$a_n = a_1 + (n-1)d$
<b><math>n^{\text{th}}</math> term of a geometric sequence</b>	In the geometric sequence with first term $a_1$ and common ratio, $r$ , the $n^{\text{th}}$ term is given by	$a_n = a_1 r^{n-1}$
<b>sum of the first <math>n</math> terms of an arithmetic sequence</b>	If an arithmetic sequence has first term $a_1$ and common difference $d$ , then the sum of the first $n$ terms is given by	$S_n = \frac{n}{2}(a_1 + a_n)$ or $S_n = \frac{n}{2}[2a_1 + (n-1)d]$
<b>sum of the first <math>n</math> terms of a geometric sequence</b>	If a geometric sequence has first term $a_1$ and common ratio $r$ , then the sum of the first $n$ terms is given by	$S_n = \frac{a_1(1-r^n)}{1-r}, \text{ where } r \neq 1$
<b>sum of the terms of an infinite geometric sequence</b>	The sum of an infinite geometric sequence with first term $a_1$ and common ratio $r$ , where $-1 < r < 1$ , is given by	$S = \frac{a_1}{1-r}$
<b><math>n</math>-factorial (<math>n!</math>)</b>	For any nonnegative integer $n$	$n! = n(n-1)(n-2)\cdots(3)(2)(1)$ and $0! = 1$
<b>binomial coefficient</b>	For nonnegative integers $n$ and $r$ , with $r \leq n$ , the symbol $\binom{n}{r}$ is defined as	$\binom{n}{r} = \frac{n!}{r!(n-r)!}$
<b>the <math>r^{\text{th}}</math> term of the binomial expansion</b>	The $r^{\text{th}}$ term of the binomial expansion of $(x+y)^n$ , where $n \geq r-1$ is	$\binom{n}{n-(r-1)} x^{n-(r-1)} y^{r-1}$
<b>binomial theorem</b>	For any positive integer $n$ : $(x+y)^n = x^n + \binom{n}{n-1} x^{n-1} y + \binom{n}{n-2} x^{n-2} y^2 + \cdots + \binom{n}{1} x y^{n-1} + y^n$	